

Centripetal Force

Any object that changes speed and/or direction has acceleration.
If there is acceleration, then there is a net force (unbalanced force) acting on the object.

For an object travelling around a circular path at a constant speed, that object will have centripetal acceleration. The net force is in the direction of the centripetal acceleration and is referred to as the centripetal force. The direction of the acceleration and thus the net force is always to the centre.

DO NOT draw F_c in your FBD..... it is essential
 \vec{F}_{net} .

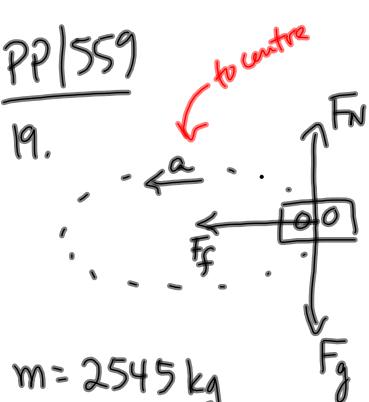
$$a_c = \frac{v^2}{r} = \frac{4\pi^2 r}{T^2} = 4\pi^2 r f^2$$

↑ period ↑ frequency

To do centripetal force problems:

- ① Draw a FBD
- ② Write the Fnet expression in $\vec{F}_{\text{net}} = m\vec{a}$
- ③ Sub in an expression for a

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$$m = 2545 \text{ kg}$$

$$V = 24 \text{ m/s}$$

$$r = ?$$

$$F_f = 1.75 \times 10^4 \text{ N}$$

$$\vec{F}_{\text{net}} = m\vec{a}$$

$$F_f = \frac{m V^2}{r}$$

$$r = \frac{m V^2}{F_f}$$

$$r = \frac{(2545 \text{ kg})(24 \text{ m/s})^2}{1.75 \times 10^4 \text{ N}}$$

$$r = 84 \text{ m}$$

If you try to turn with a radius of less than 84m, you

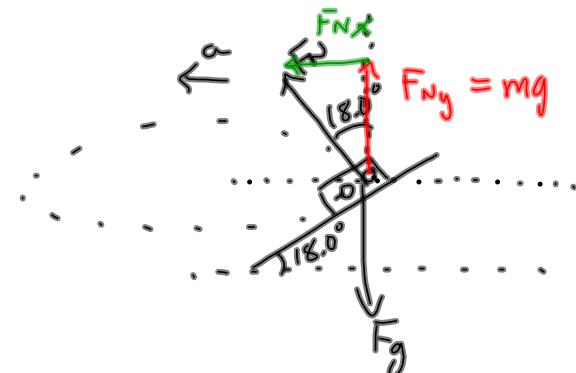
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$$r = 382 \text{ m}$$

$$\theta = 18.0^\circ$$

frictionless

$$V = ?$$



$$\tan \theta = \frac{F_{N_x}}{F_{N_y}}$$

$$F_{N_x} = F_{N_y} \tan \theta$$

Vertically:

$$F_{N_y} = F_g$$

$$F_{N_y} = mg$$

Horizontally:

$$\vec{F}_{\text{net}} = m \vec{a}$$

$$F_{N_x} = m \frac{v^2}{r}$$

$$F_{N_y} \tan \theta = \frac{m v^2}{r}$$

$$mg \tan \theta = \frac{m v^2}{r}$$

$$378.11 \frac{\text{km}}{\text{h}} \left(\frac{1000 \text{m}}{1 \text{km}} \right) \left(\frac{1 \text{h}}{3600 \text{s}} \right)$$

$$= 105 \frac{\text{m}}{\text{s}}$$

\uparrow
must be friction in order
to reach this speed.

$$v^2 = gr \tan \theta$$

with no friction \rightarrow

$$v^2 = (9.81 \text{m/s}^2)(382 \text{m}) \left(\tan 18.0^\circ \right)$$

$$v = 34.9 \text{ m/s}$$

To DU
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